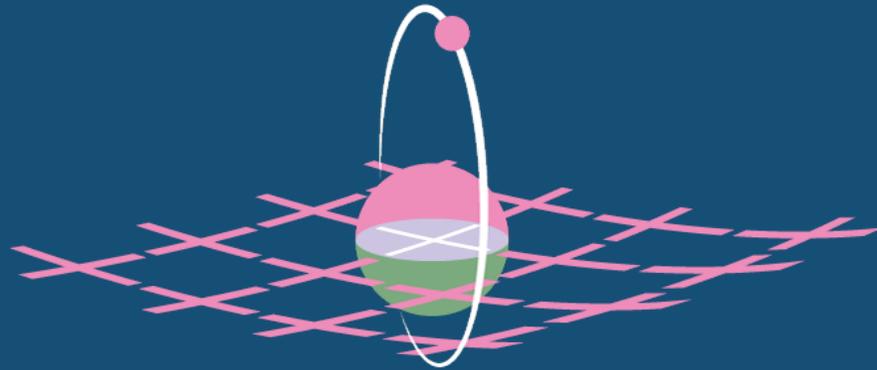
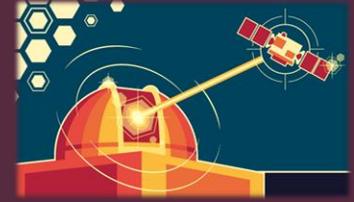


22nd International Workshop on Laser Ranging, 7-11
November 2022, Guadalajara, Spain



METRIC

MEASUREMENT OF ENVIRONMENTAL AND
RELATIVISTIC IN-ORBIT PRECESSIONS

**METRIC: a compact mission
concept for upper atmosphere
mapping, fundamental physics
and geodesy**



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Science for a safer land



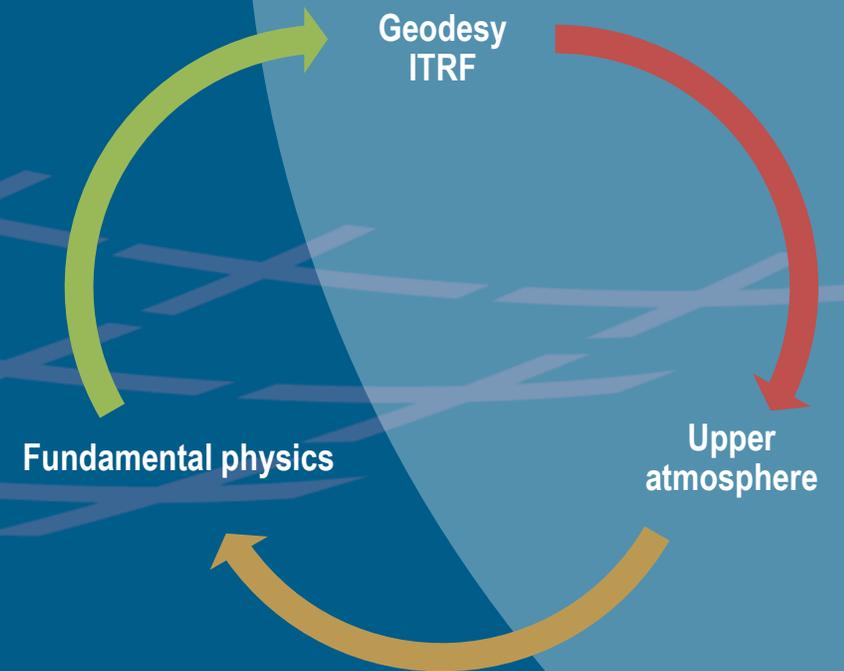
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METRIC scientific objectives

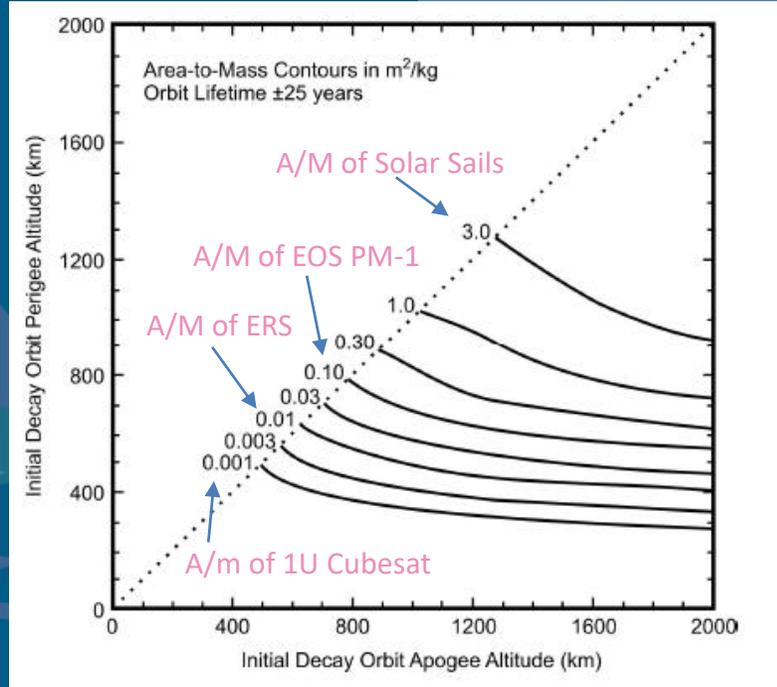
METRIC: Measurement of Environmental and Relativistic In-orbit preCessions

- **Upper atmosphere** Map **atmospheric density** by in-situ **acceleration measurement**, together with SLR and GNSS tracking, at altitudes of interest for satellite deorbiting, upper atmosphere modelling, orbital debris
- **Fundamental physics** Tests of **gravitation theories** in weak-field conditions through a precise measurement of **nodal and apsidal lines precession**
- **Geodesy / ITRF** Provide a space-based **core co-location site** for linking space geodetic techniques



Science – Upper Atmosphere Density Mapping

S/C lifetime 25 years: NASA, 1995



- **Goal** Accurate measurements of **atmospheric drag** in the altitude range where it affects **satellite lifetimes** (**Peron & Lorenzini 2014**)
- **Issues**
 - Satellites in the range 450-1200 km of altitude may or may not violate the **25-year deorbit guideline** depending on ballistic coefficient and solar activity
 - Knowledge of **atmospheric density** and its dependency on varying solar and geomagnetic activity is still affected by large uncertainties, especially in upper-LEO (**Pardini+ 2001, 2006, 2010, 2012**)
- **Returns** Improved knowledge of atmospheric density and its variability in LEO will benefit the **estimate of satellites lifetimes** and the **accuracy of conjunction assessments**. Any progress in the field will lead to a reduction of **collision avoidance maneuvers**, saving **propellant**, improving **safety**, mitigating the problems related to **orbital debris**

Science – Fundamental Physics

Relativistic corrections to geocentric equations of motion – IERS Conventions (2010)

The test of the **equation of motion** for a massive body in a given gravitational field remains an important tool in the quest for a unified description of the fundamental interactions in the physical universe

$$\Delta \ddot{\vec{r}} = \frac{GM_E}{c^2 r^3} \left\{ \left[2(\beta + \gamma) \frac{GM_E}{r} - \gamma \dot{\vec{r}} \cdot \dot{\vec{r}} \right] \vec{r} + 2(1 + \gamma)(\dot{\vec{r}} \cdot \dot{\vec{r}}) \dot{\vec{r}} \right\} + (1 + \gamma) \frac{GM_E}{c^2 r^3} \left[\frac{3}{r^2} (\dot{\vec{r}} \times \dot{\vec{r}})(\dot{\vec{r}} \cdot \vec{J}) + (\dot{\vec{r}} \times \vec{J}) \right] + \left\{ (1 + 2\gamma) \left[\dot{\vec{R}} \times \left(\frac{-GM_S \dot{\vec{R}}}{c^2 R^3} \right) \right] \times \dot{\vec{r}} \right\},$$

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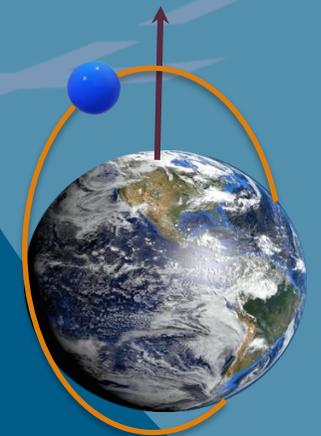
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Effect	Ratio to J_0
Schwarzschild	$10^{-9} - 10^{-10}$
Lense-Thirring	$10^{-11} - 10^{-12}$
De Sitter	$10^{-11} - 10^{-12}$

	METRIC	LAGEOS
e	5.2×10^{-2}	4.43×10^{-3}
$\dot{\omega}_{Schw}$	12.5	3.28
$\dot{\Omega}_{LT}$	0.153	0.0309
$\dot{\omega}_{LT}$	~ 0	0.0314
$\dot{\Omega}_{dS}$	0.0176	0.0176
$\dot{\omega}_{Yuk}$	(0.144)	(0.0819)

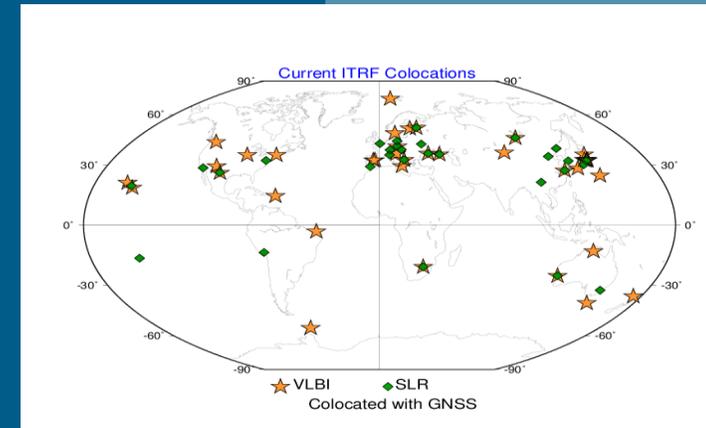
Relativistic secular precession rates (arcsec/year)

Advantages of a **polar or quasi-polar orbit**: strong suppression of competing **Newtonian gravitational signal**



450 x 1200 km polar orbit

SLR & VLBI are critical for the ITRF frame definition : origin (SLR), scale (SLR & VLBI), but their co-locations (< 10 sites) are poorly distributed



- The ITRF is fundamentally based on **co-locations** of 2 or more instruments operating at the same site, and with terrestrial ties available
- Almost all SLR, VLBI and a large number of DORIS stations are co-located with GNSS
- → **GNSS links together SLR, VLBI & DORIS networks**
- But more than 50 % of tie discrepancies are larger than 5 mm, caused mainly by **technique systematic errors**

Objective

Co-locating all four technique instruments at one **fully calibrated satellite-based platform**, a **“Core co-location site in space”** is expected to mitigate/cancel technique systematic errors and thus improves the ITRF accuracy

Basic mission idea

Core on-board instrumentation (baseline)

- **3-axis accelerometer** for **NGP** measurement
- Corner cube **laser retroreflectors** for **SLR**
- **GNSS** receiver
- Vacuum pressure ion-gauge

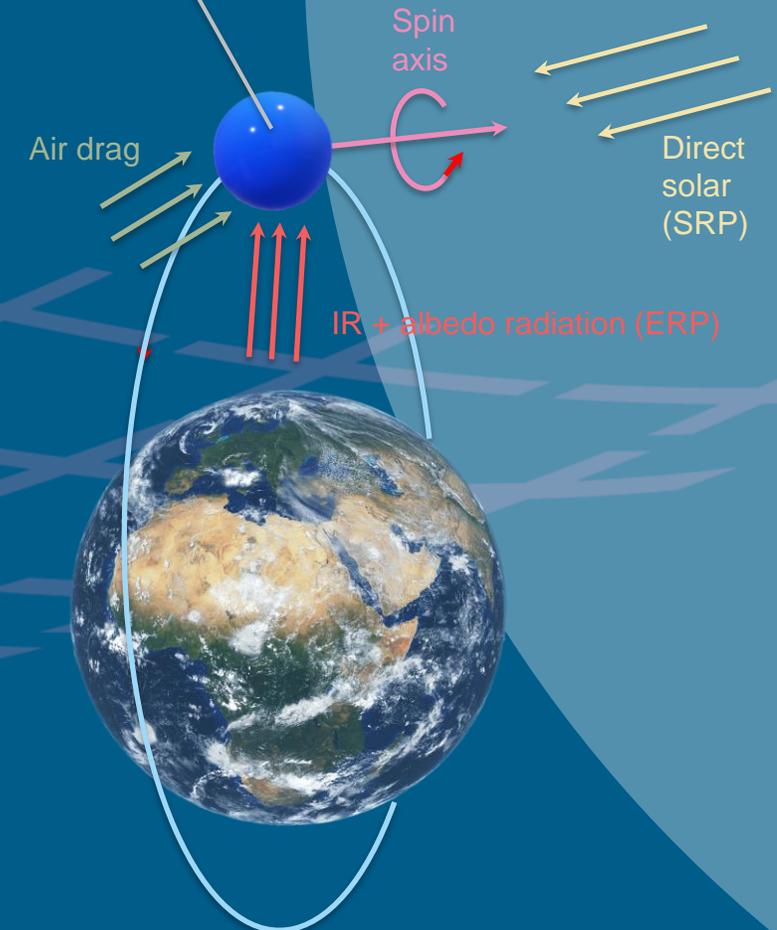
Strategy

- **Polar eccentric orbit (preliminary: 400/450 km x 1200 km)**
- Tracking with at least two **space geodetic techniques**
- **Virtual drag-free** spacecraft through acceleration data
- Modulation of acceleration signal via **slow spin**
- Separation of atmospheric drag and solar radiation pressure is achieved by means of acceleration measurement near apogee

International context

- **Upper atmosphere** Strong need for **reliable upper atmosphere density models** (satellite lifetime, collision avoidance maneuvers)
- **Fundamental physics** Testing the law of **gravitation** (general relativity vs alternative theories)
- **Geodesy / ITRF**: Requirement of a more accurate **terrestrial reference frame** from a host of disciplines (astronomy, navigation, Earth System sciences) – Complementary and synergistic with the ESA GENESIS programme

Body-mounted solar arrays and laser retroreflectors

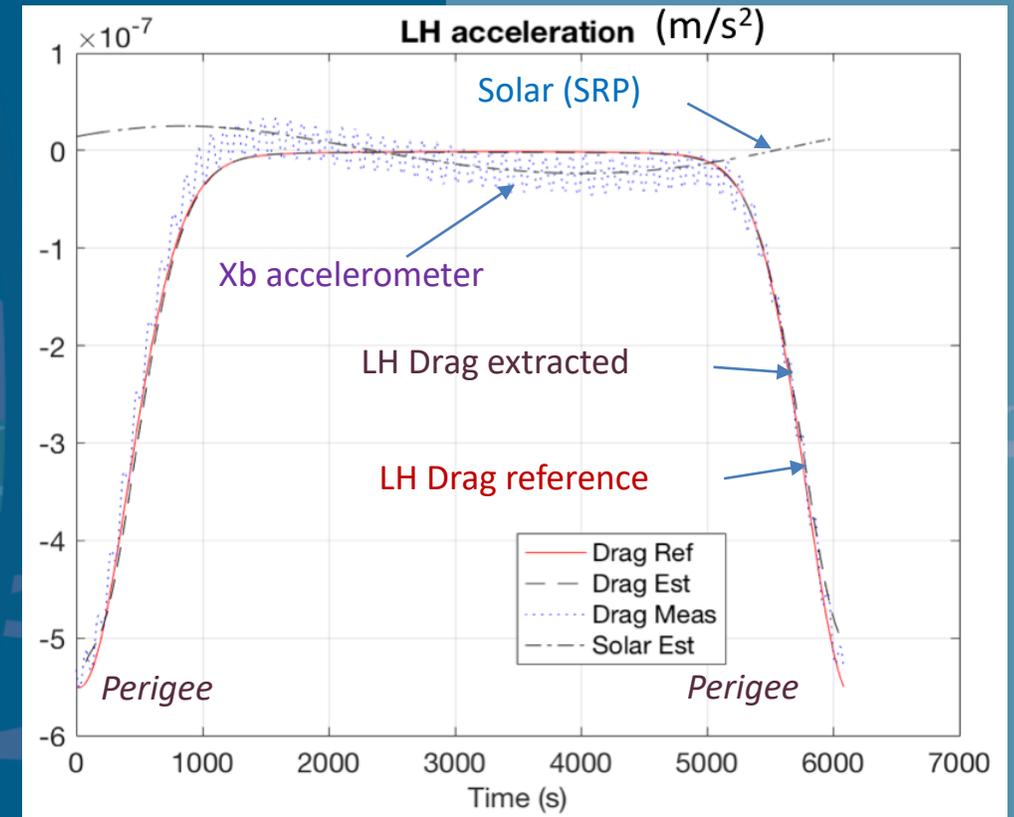


Atmospheric drag vs solar radiation pressure

The proposed strategy enables a clear separation between atmospheric drag and solar radiation pressure:

- Drag overpowers solar acceleration below an altitude of ~ 600 km (close to perigee)
- Solar radiation pressure is > 20 times stronger than drag at 1200 km of altitude (close to apogee)
- Direct solar radiation acceleration on a sphere can be modelled accurately and has a long time scale
- Earth radiation acceleration is variable on a shorter time scale but it acts in the local vertical (LV) component in phase quadrature with respect to the major atmospheric drag component along local horizontal (LH)

Acceleration – LH comp.	Range (m/s ²)	Remarks
Neutral Drag	-1×10^{-9} to -5.5×10^{-7}	The “signal” for atmo. drag
Solar Radiation Pressure	-2.5×10^{-8} to 2.5×10^{-8}	Removed through measurement at apogee
Satellite spin motion	2.7×10^{-6}	At coning motion frequency and is filtered out

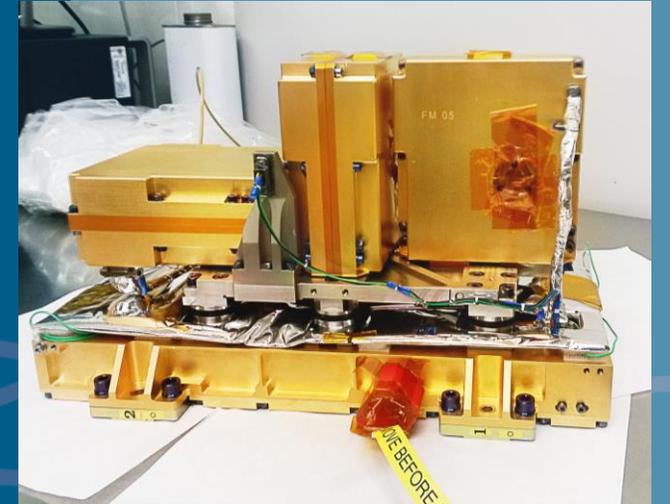


Adapted from **Lorenzini & Peron 2018**

Accelerometer

Heritage

- Original instrument concept developed at INAF-IAPS:
 - Mass-spring sensitive element with electrostatic read-out and actuation systems
 - Three-axial configuration
- ASI-INAF-TAS-I scientific payloads developed for ESA missions:
 - **ISA (Italian Spring Accelerometer)** is operating onboard **BepiColombo**
 - **HAA (High Accuracy Accelerometer)** will fly onboard **JUICE**
- Know-how @INAF-IAPS about:
 - On-ground and in-flight calibration
 - In-flight operations management
 - Data handling, archiving and analysis



METRIC accelerometer requirements:

- Signal dynamics: 10^{-6} m/s²
- Measurement band: 10^{-4} – 10^{-1} Hz
- Precision: 10^{-10} m/s²

ISA/HAA performance (as reference):

Signal dynamics	3×10^{-6} m/s ²
Measurement band	3×10^{-5} – 10^{-1} Hz
Precision	10^{-8} m/s ² for signal amplitude $\leq 3 \times 10^{-6}$ m/s ²
Noise floor	3×10^{-8} m/s ² /√Hz @f > 10^{-4} Hz

METRIC requires about 2 orders of magnitude improvement over ISA; this is considered achievable relying on ongoing development activities (INAF-TAS-I cooperation)

Laser Retroreflector Array (LRA): preliminary, by INFN-LNF

- Designed/supplied by INFN-Frascati, which has a vast experience in LRAs for:
 - LEO, Earth Observation altitudes to MEO (**LARES 2**, 2022)
 - Galileo** 2nd Generation (G2G) for Thales Alenia and Airbus (2023-2025)
 - The **Moon**: for ESA and a NASA-CLPS flight (2024)
 - Mars (2016-2020), Phobos, Hera @ Didymos, etc.
- Given METRIC low altitude/eccentric polar orbit, 450×1200 km (preliminary), technology will likely be an LRA of metal-coated fused silica reflectors (CCRs)
 - Heritage: NASA-ESA-ASI Mars surface missions (ExoMars, InSight, Perseverance)
 - Alternative: LRA / CCR technologies are also under consideration
- CCR class: COTS, with reduced procurement time and very consolidated heritage from two LARES 2 satellites for ASI (606 CCRs), 1st flown on Vega C
- LRA distributed on METRIC sphere, filling ~ 50% (w/solar panels), as homogeneous and isotropic as possible/allowed by s/c system constraints
- CCR detailed specs (including exact diameter), total #: to be optimized vs mass/volume
- If SLR at culmination important, then small(er) CCR diameter favored
- Target SLR accuracy: 1 cm, or better

Miniature LRAs for the **Perseverance** roving Mars (built by INFN-LNF)



LARES 2 (built by INFN-LNF and INFN-Padova)



Extended configuration

Atomic clock

- Possibly solid-state (e.g., Cesium clock: Allan variance $\sim 10^{-13}$ s/s)
- Scientific returns using a Doppler canceling technique: gravitational redshift measured over many revolutions

VLBI beacon

- Not trivial (i.e. considering a radio beacon at a finite distance) and must be carefully assessed, together with the observing frequency range and the network of stations tracking the satellite
- A new generation of instruments, VLBI Global Observing System (VGOS), has been established in order to meet the scientific requirements set by GGOS (i.e. an accuracy of 1 mm in station position and 0.1 mm/year in station velocity on a global scale)



Spacecraft – Preliminary estimates

Satellite characteristics at a conceptual design level

- Spherical outer shape with diameter: 50-60 cm
- Estimated overall power consumption: < 30-40 W
- Multi-junction, body-mounted solar arrays
- Satellite estimated mass range: 100-200 kg (inclusive of ballast to trim ballistic coefficient)
- Spin-stable: inertia tensor of S/C is non spherical and spin is around principal inertia axis
- Magnetorquers for coning control and sporadic spin trimming
- Cold gas system planned for spin-up
- **Mission duration: ideally 11 years (one solar cycle), or shorter with possible extension**

TRL preliminary estimates of main elements

- Accelerometer and laser retroreflectors: ≥ 7 (tested in space in other configurations)
- Ion Vacuum gauge: 6 (commercial product to be tested for space use)
- GNSS receiver and antennas: ≥ 7 (already used in space)
- Spacecraft: 2 (presently at conceptual level)

Italian reference community



- **INAF-IAPS** High-sensitivity accelerometers development / calibration / operation (ground and space), precise orbit determination, satellite dynamics modelling, general relativity
- **INAF-IRA** Geodetic VLBI observation design / realization / data analysis, GNSS data analysis, local ties
- **INAF-OATo** Astronomical instrumentation modelling, data reduction and analysis algorithms, gravity theories and their experimental tests, relativistic astrometry modelling, high-performance computing, big data and numerical methods
- **UniPD-CISAS** Mission analysis, measurements in space, scientific instruments onboard accommodation
- **UniPD-DII** Contributions to satellite design
- **UniPD-GEO** GNSS data analysis, general relativity
- **CNR-ISTI** Upper atmosphere drag modelling
- **INFN-LNF** Laser retroreflectors and their accommodation
- **IGN-LAREG** ITRF maintenance, geodetic co-location
- **ASI-CGS** LLR, SLR, geodesy
- **YETITMOVES** GNSS data analysis
- **UniRoma2** Post-flight data analysis
- **TAS-I** High-sensitivity accelerometers space engineering and production



Scientific objectives and mission concept

- Contribution to **three** different scientific domains
- Integration of (well) known instruments and techniques

Complementarity and synergy with ESA GENESIS programme

- **Orbit** Lower and eccentric
- **Mission duration** Should cover ideally one solar cycle
- **Geodesy / ITRF** Co-location of two/three techniques
- **NGP** Signal or (removed) noise depending on the objective (the accelerometer being one of the core instruments)
- **Spacecraft** Very compact, simple external geometry, **high-precision metrology** being a design driver

Conclusions

Essential features

- High-accuracy **accelerometer** package
- Accurate **tracking** of spacecraft
- **Polar eccentric orbit** spanning the 400/450 × 1200 km altitude range
- Spacecraft slowly spinning about an axis perpendicular to the orbital plane
- Simple spacecraft external geometry

Expected improvements to science/technology

- **Upper atmosphere** Atmospheric drag and solar radiation pressure in-situ measurement with accurate accelerometer and vacuum pressure ion-gauge over an altitude span of great interest to atmospheric science, satellite technology, orbital debris mitigation
- **Fundamental physics** A polar eccentric orbit with a clear definition of the perigee and a virtually drag-free spacecraft will lead to a precise measurement of apsidal and nodal lines precession
- **Geodesy / ITRF** Co-located position measurements with SLR + GNSS (+ VLBI) will provide a space-based core co-location site

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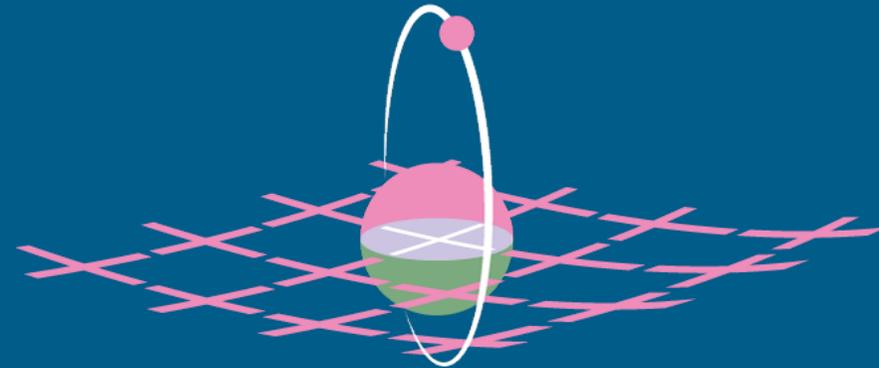
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THANKS for your attention

Questions?

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